



Студенттер мен жас ғалымдардың
«ҒЫЛЫМ ЖӘНЕ БІЛІМ - 2018»
XIII Халықаралық ғылыми конференциясы

СБОРНИК МАТЕРИАЛОВ

XIII Международная научная конференция
студентов и молодых ученых
«НАУКА И ОБРАЗОВАНИЕ - 2018»

The XIII International Scientific Conference
for Students and Young Scientists
«SCIENCE AND EDUCATION - 2018»



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The proceedings are the papers of students, undergraduates, doctoral students and young researchers on topical issues of natural and technical sciences and humanities.

В сборник вошли доклады студентов, магистрантов, докторантов и молодых ученых по актуальным вопросам естественно-технических и гуманитарных наук.

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WEIGHTED HARDY TYPE INEQUALITY ON TIME SCALE

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For completeness, before we prove the main results, we recall the following concepts related to the notion of time scales.

A *time scale* T is an arbitrary nonempty closed subset of the real numbers. Thus

$$R, Z, N, N_0,$$

i.e., the real numbers, the integers, the natural numbers, and the nonnegative integers are examples of time scales, as are

$[0;1]$, $[2;3]$, $[0,1] \cup N$ and the Cantor set;

while

$$Q, R \setminus Q, (0; 1),$$

i.e., the rational numbers, the irrational numbers, the complex numbers, and the open interval between 0 and 1, are not *time scales*.

The calculus of time scales was initiated by Stefan Hilger in his PhD thesis [1] in order to create a theory that can unify discrete and continuous analysis. Indeed, below we will introduce the delta derivative f^Δ for a function f defined on T , and it turns out that

(i) $f^\Delta = f'$ is the usual derivative if $T = R$ and

(ii) $f^\Delta = \Delta f$ is the usual forward difference operator if $T = Z$.

Let T be a time scale. For $t \in T$ we define the forward jump operator $\sigma: T \rightarrow T$ by

$$\sigma(t) := \inf\{s \in T; t < s\},$$

while the backward jump operator $\rho: T \rightarrow T$ is defined by

$$\rho(t) := \inf\{s \in T; s < t\}.$$

If $\sigma(t) > t$, we say that t is right-scattered, while if $\rho(t) < t$ we say that t is left-scattered. If $t < \sup T$ and $\sigma(t) = t$, then t is called right-dense, and if $t > \inf T$ and $\rho(t) = t$, then t is called left-dense. Points that are right-dense and left-dense at the same time are called dense.

Definition 1. Assume $f: T \rightarrow R$ is a function and let $t \in T$. Then we define $f^\Delta(t)$ to be the number (provided it exists) with the property that given any $\varepsilon > 0$, there is a neighborhood U of t (i.e., $U = (t - \delta; t + \delta) \cap T$ for some $\delta > 0$) such that

$$|[f(\sigma(t)) - f(s)] - f^\Delta(t)[\sigma(t) - s]| < \varepsilon |\sigma(t) - s|.$$

We call $f^\Delta(t)$ the delta (or Hilger) derivative of f at t .

Definition 2. A function $f: T \rightarrow R$ is called regulated provided its right-sided limits exist (finite) at all right-dense points in T and its left-sided limits exist (finite) at all left-dense points in T .

Definition 3. A function $f: T \rightarrow R$ is called rd-continuous provided it is continuous at right-dense points in T and its left-sided limits exist (finite) at left-dense points in T .

We define the indefinite integral of a regulated function f by

$$\int f(t) \Delta t := F(t) + C,$$

where C is an arbitrary constant and F is a pre-antiderivative of f . We define the Cauchy integral by

$$\int_a^b f(t)\Delta t := F(b) - F(a),$$

for all $a, b \in T$. A function $F : T \rightarrow R$ is called an *antiderivative* of $f : T \rightarrow R$ provided $F^\Delta(t) = f(t)$ holds for all $t \in T$.

Denote $[a; \infty)_T := \{t \in T : t \geq a\}$, where T is a particular time scale, which is unbounded above. For $\forall a \in R$ the set of rd-continuous functions $f : [a; \infty)_T \rightarrow R$ will be denoted by $C_{rd}[a; \infty)_T$.

We consider an integral inequality in the following form:

$$\left(\int_a^\infty u^q(x) \left(\int_a^x f(t)\Delta t \right)^q \Delta x \right)^{1/q} \leq C \left(\int_a^\infty f^p(x) v^p(x) \Delta x \right)^{1/p}, \quad \forall f \in C_{rd}[a; \infty)_T, \quad (1)$$

where the constant C does not depend on function f , and $p; q$ are fixed parameters and u and v be nonnegative weight functions. If $T = R$, then we get that the well known classical weighted Hardy type inequality was studied by the books [2], [3], [4] and [5].

Our main result reads as follows.

Theorem 1. *Let $1 \leq p \leq q < \infty$ and $\frac{1}{p} + \frac{1}{p'} = 1$. Then the inequality (1) holds if and only if $B < \infty$ satisfied, where*

$$B := \sup_{t \in [a; \infty)_T} \left(\int_t^\infty u^q(x) \Delta x \right)^{1/q} \left(\int_a^t v^{-p'}(\tau) \Delta \tau \right)^{1/p'} < \infty,$$

Moreover, $B \approx C$, where C is the best constant in (1).

References

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TWO-WEIGHTED ESTIMATES FOR RIEMANN-LIOUVILLE INTEGRAL ON TIME SCALE

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Since the discovery of the classical Hardy inequalities (continuous or discrete) much work has been done, and many papers which deal with new proofs, various generalizations and